

① Data types to
model interactive
applications } HW6

② Polymorphism } HW7

Idea:

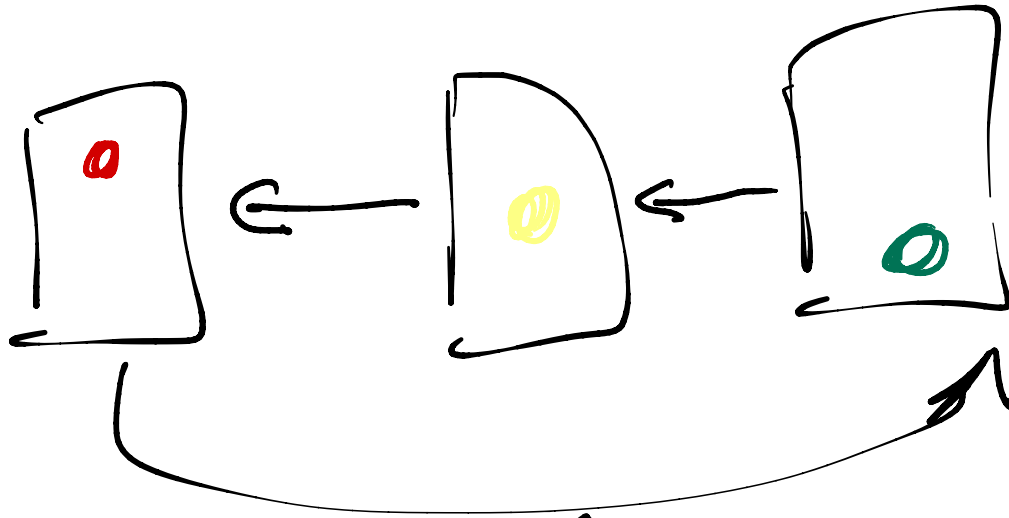
model interactive
time-varying application

as state-transition system



Traffic light

States



time

transitions

model - view - controller paradigm

separate

- ① "data model"
- ② view
- ③ responding to input/time/...

datatype model = Red
 | Green
 | Yellow } states

① view(s)
 ↳ web/ios/android/native....

② transition model

fun view(m: model): String =

case m of

Red => "  "

| ~~Yellow~~ => "  "

| Green => "  "



(* respond to time *)
fun respond(m: model) : model =
 case m of
 Red $\Rightarrow$ Green
 | Yellow $\Rightarrow$ Red
 | Green $\Rightarrow$ Yellow

says the "logic" in terms
of the data model

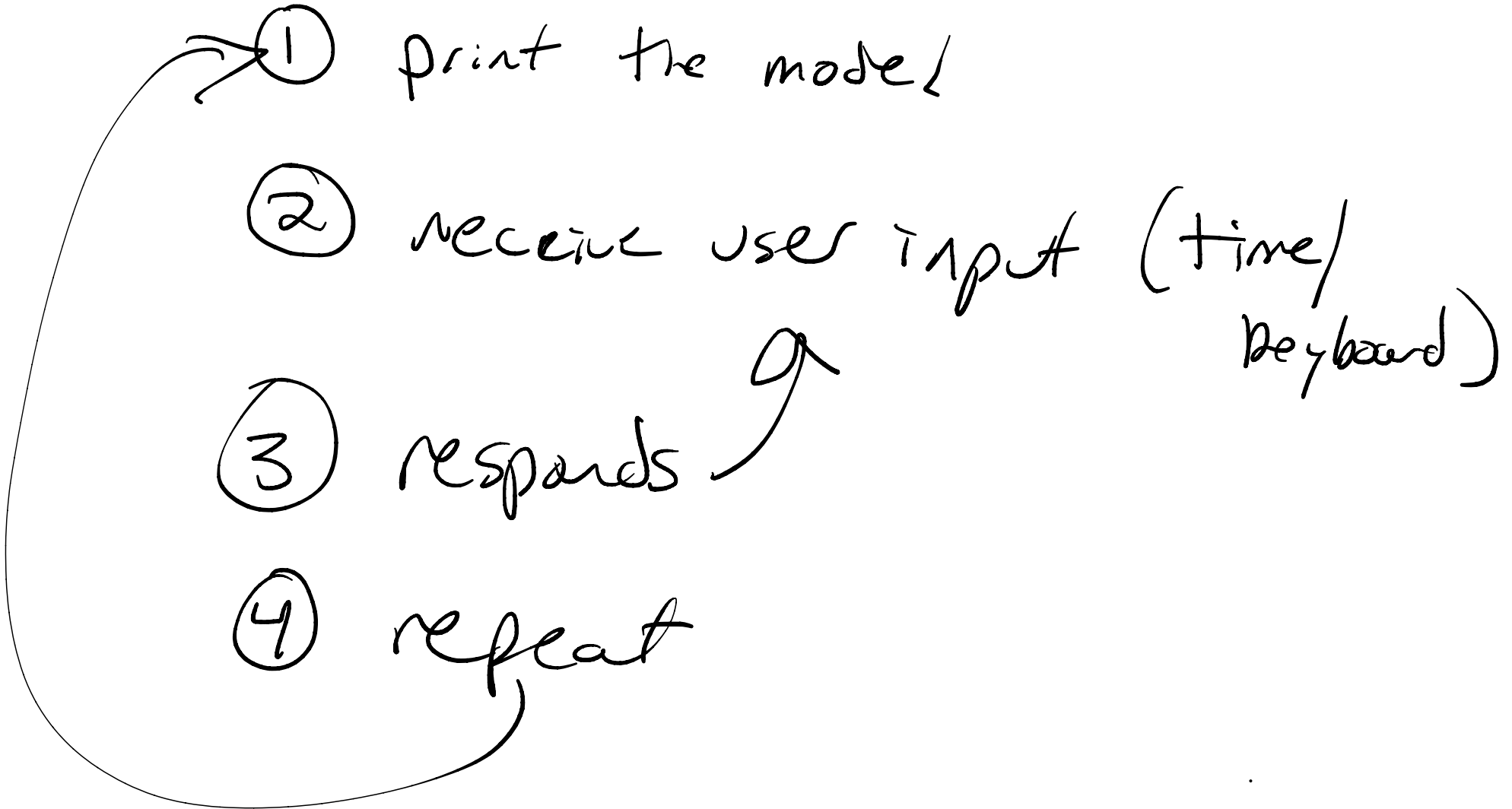
Controller:

① print the model

② receive user input (time/
keyboard)

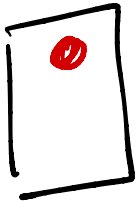
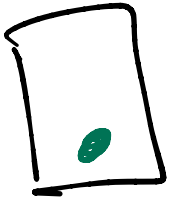
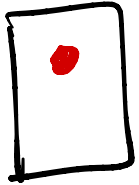
③ responds

④ repeat



Controller (view, respond, Red);

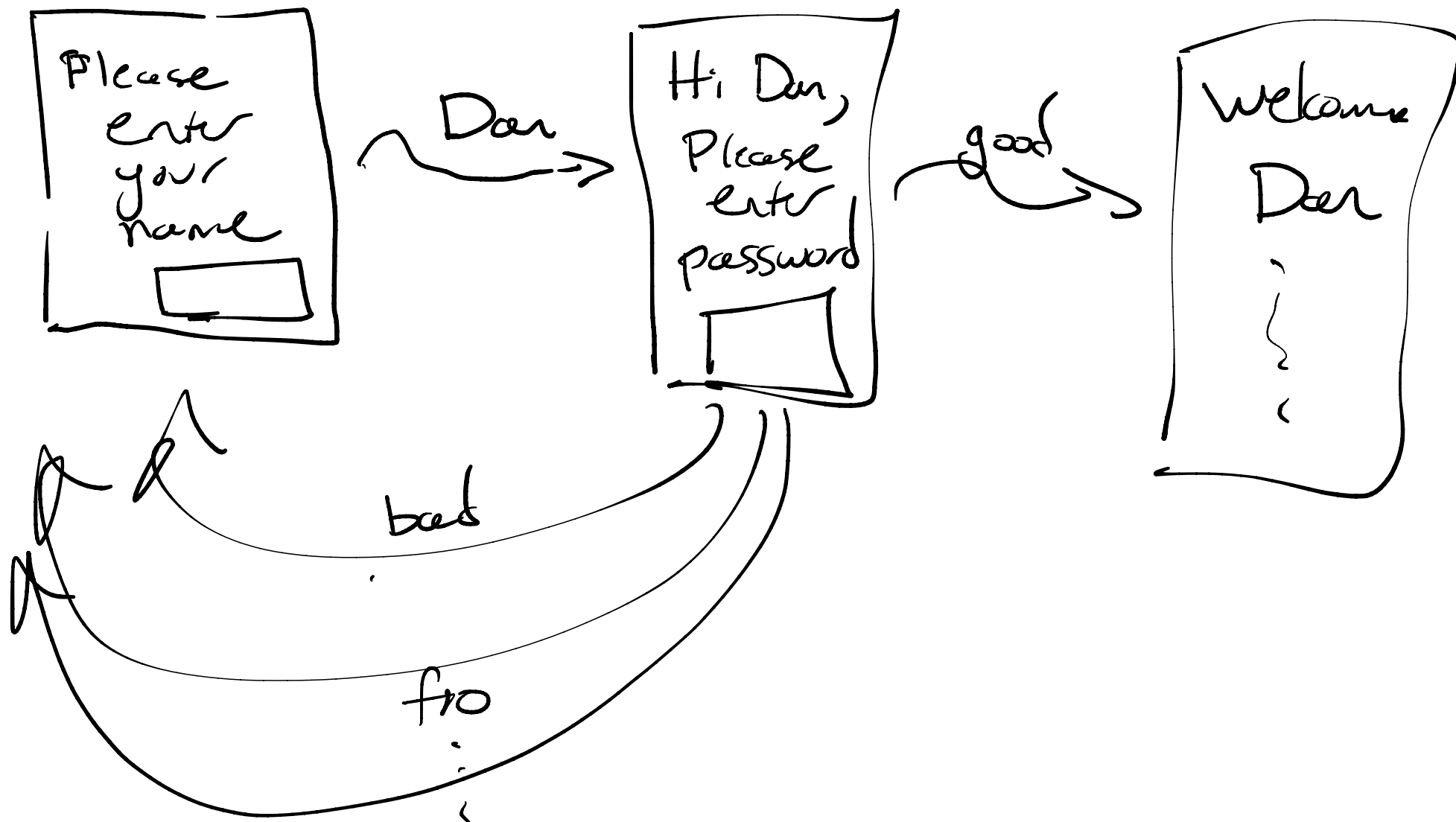
↑
which state
to start in

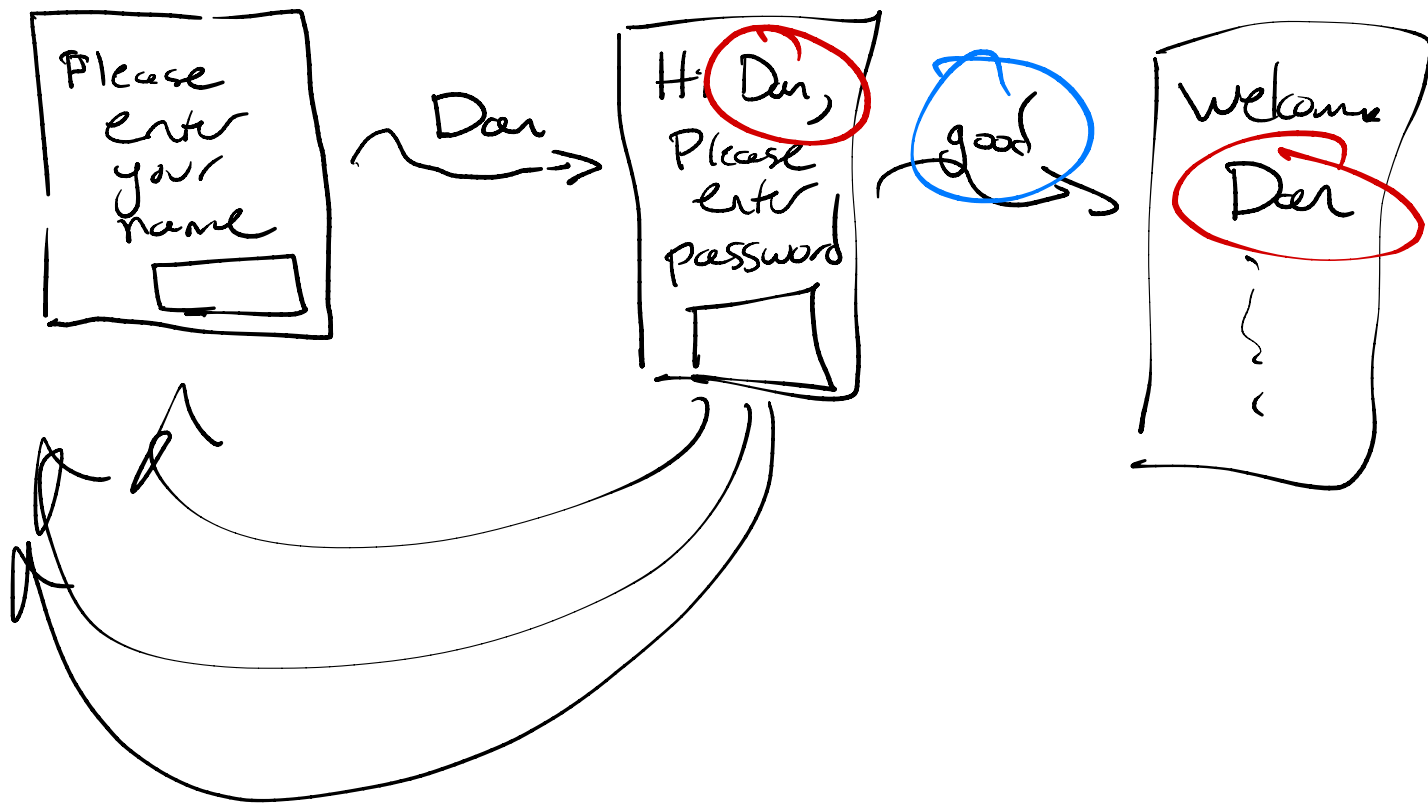


...

- ① model datatype
 - ② view
 - ③ respond
 - ④ initial state
 - ⑤ controller
- } specific to application

Model with data: login prompt





name
for
state

EnterName

EnterPassword

loggedIn

data nothing

name

name

name
for
state

EnterName

EnterPassword

LoggedIn

data nothing

name

name



datatype model = EnterName

| EnterPassword of String

| LoggedIn of String

datatype int list = ^{x::xs} 30 of 'int * int list

respond

view

initial State

Enter Name

```
fun view(m: model): string = case m of
  EnterName => "Please enter your name:"
| EnterPassword(name) => "Hi " ^ name ^
  "Please enter password:"
| LoggedIn(name) =>
  "Welcome" ^ name ^ "..."
```

fun respond(m: model, input: string): model =
case m of

EnterName => EnterPassword(input)

| EnterPassword(name) => password

(case checkPassword(name, input) of
true => LoggedIn(name)
| false => EnterName)

| LoggedIn(name) => ...

HW6:

Shopping cart

Abstracting repeated code



Single point of
control

Poly morphism

→ Same code can work
at many types

An int list is

$[]$ or

$x :: xs \quad x : \text{int}$
 $xs : \text{int list}$

An string list is

$[]$ or

$x :: xs \quad x : \text{string}$
 $xs : \text{string list}$

variable
type

An 'a list is

$[]$

$x :: xs \quad \text{where } x : 'a$
 $xs : 'a \text{ list}$

```

fun length(l: int list): int =
  case l of
    [] => 0
  | x::xs => 1 + length(xs)

```

```

fun length(l: String list): int =
  case l of
    [] => 0
  | x::xs =>
    1 + length(xs)

```

length [1, 2, 3]

$\wedge$
 $\alpha = \text{int}$

length ["a", "b"]

$\wedge$
 $\alpha = \text{String}$

works for any type α

✓

```

fun length(l:  $\alpha$  list): int =
  case l of
    [] => 0
  | x::xs => 1 + length(xs)

```

fun sum(l: ^{doesn't type check} 'a' list): int = because
case l of
 [] => 0
 (int (real))

| x :: xs => ^{'a'} x + sum(xs)

$\text{for any } 'a \xrightarrow{\text{str}}_{\text{int}}$ $\text{for any } 'b \xrightarrow{\text{str}}_{\text{int}}$

$\text{fun zip}(l_1: ('a) \text{ list}, l_2: ('b) \text{ list}): ('a * 'b) \text{ list} =$

case (l_1, l_2) of

$([], _) \Rightarrow []$

$| (_, []) \Rightarrow []$

$| (x::xs, y::ys) \Rightarrow (x, y) :: \text{zip}(xs, ys)$

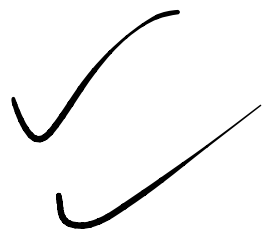
$\text{zip}(\underline{[1, 2, 3]}, \underline{["a", "b", "c"]})$

$1a = \text{int}$

$'b = \text{str}$

$\text{zip}(["a"], ["d"])$

$\text{zip}([1, 2, 3], (4, 5, 6))$



^{for any}
 fun append($l_1: 'a$ list, $l_2: 'a$ list): $'a$ list =
 case l_1 of
 $() \Rightarrow l_2$

^{'a}
 $| x :: xs \Rightarrow x :: \text{append}(xs, l_2)$
 _{$'a$}

$\text{append}_\Lambda([1, 2, 3], ["a", "b"]) = ???$

$'a = \text{int}$
 $'b = \text{string}$

Type inference

fun append(l_1 , 'd list, l_2 , 'd list) 'd list =

case l_1 of

$() \Rightarrow$ l_2

| $x :: xs \Rightarrow$ $x :: \text{append}(xs, l_2)$

a = 'd list

'b = 'c

'c = 'd list

Solve equations