COMP 212 Fall 2024 Homework 10

In this homework, you will implement a parallel programming abstraction called *extract-combine*, which is the essence of cluster-programming techniques like Hadoop and Google's MapReduce.

You will use extract-combine to program a simple machine learning algorithm called naïve Bayes classification, and use this classification algorithm to automatically label news articles with categories (such as "economics" or "government/social"); another typical application is spam filtering, labeling an email with categories "spam" or "not spam". The first phase of classification is training, where word frequency counts are extracted from a collection of documents that have been labeled with categories. In the next phase, these frequencies are used to predict the category for unlabeled documents. Naïve Bayes classification is called "naïve" because it treats a document as a multiset of words, ignoring the order of the words and other dependencies. It is called "Bayes" because a fact about probabilities called Bayes' rule is the main component of the method.

1 Extract-combine

For many data analysis tasks, the input is a large collection of *documents* of some sort, which we call a *dataset*. Here, we will use a dataset whose documents are Reuters news articles:

England midfielder Paul Gascoigne stunned Hearts with two goals in 90 seconds...

The Stock Exchange of Singapore said on Tuesday that a technical fault...

One common pattern for processing such a dataset is to

- 1. extract some information from each document, and then
- 2. combine the extracted information from all documents

It is often convenient if the extraction phase produces a sequence of key-value pairs (where a particularl key can occur more than once in the sequence), and the combination phase combines these pairs into a dictionary.

For example, suppose we want to count the frequencies of each word in the following dataset, which has two documents:

```
this is is document 1
```

this is document 2

We would

1. Extract from each document the sequence of pairs (w, 1) for each word in the document:

```
("this",1)
("is",1)
("is",1)
("document",1)
("1",1)

("this",1)
("is",1)
("document",1)
("document",1)
("2",1)
```

2. Combine these pairs into a dictionary mapping words to numbers, by adding the values associated with each word:

```
"1" ~ 1
"2" ~ 1
"document" ~ 2
"is" ~ 3
"this" ~ 2
```

This suggests a higher-order function

This first input is a comparison function ordering some type of keys 'k. The second input is the *extractor*, which extracts a key-value sequence from a document, where a single document is represented by a type 'a. The third input is the *combiner*, which is used to combine values (which have type 'v) when the same key occurs multiple times in the extracted information. The fourth input is a sequence of documents. The output is a key-value dictionary consisting of all of the keys extracted from all of the documents, where the dictionary maps a key to the combination of all of its extracted values.

For example, for frequency counting, suppose where are given a sequence of documents, where each document is a single string. Then we can do

Here we assume that the function words divides a string into words. The extractor pairs every word in a document with 1, and the combiner is addition. The resulting function creates a dictionary with the frequencies of all of the words in all of the documents.

1.1 Data source

For many applications of extract-combine, each individual entry in the input dataset is not very large, but the overall number of documents is big, so that the size of the entire dataset is megabytes or gigabytes or more.

The above type for extractcombine assumes a sequence (Seq.seq) of documents as an input. Since an 'a Seq.seq is represented by a value in memory (RAM), this means that to use extractcombine, we first need to load the entire dataset as a value in memory. However, for many applications, the information being collected from the data is much smaller than the dataset itself. For example, when we count word frequencies, the output is proportional to the number of unique words in the documents, which will likely be much less than the total number of words in the documents. Thus, we should be able to process a collection of documents that is too big to fit in memory, as long as the number of unique words fits. But to do this, we need to generalize extractcombine so that it does not require its input to be in memory.

At a first cut, what we want is another implementation of the SEQUENCE signature, whose values are stored as a file on disk instead of as a value in memory. However, for this problem, we will not need these disk-based sequences to support all of the sequence operations: in particular, we never need to *create* such a sequence (via tabulate or map), we only need to *consume* them. Indeed, the only operation we need is mapreduce, so we define the following signature:

¹If the extracted information does not fit in memory, it too can be stored on disk, but we won't pursue that here.

end

A type is *mapreducable* if it has a mapreduce function. The prototypical mapreducable type is 'a Seq.seq, which is expressed by the following instance:

```
structure SeqMR :> MAP_REDUCE where type 'a mapreducable = 'a Seq.seq =
struct
    type 'a mapreducable = 'a Seq.seq
    fun mapreduce (1, e, n, s) = Seq.mapreduce (1, e, n, s)
end
```

The homework support code also defines a second instance FileMR that reads from a file:

```
structure FileMR : MAP_REDUCE
```

The idea is that 'a FileMR.mapreducable reads values of type 'a from a file, and the mapreduce function does a map-reduce on all of the values in a file.

For the remainder of the homework, we will assume that there is a

```
structure MR : MAP_REDUCE
```

defining a mapreducable type, which will be either SeqMR or FileMR from above, depending on which CM file is used to compile the project. You should use MR.mapreduce to refer to the mapreduce function for either sequences or files in your code. Like the two plane implementations in Barnes Hut, this will allow you to test the code using both sequences (for small tests written in the SML files) and using data read from a file.

1.2 Task

Your job is to implement the extract-combine pattern as a function with the following type (see extractcombine.sig):

```
signature EXTRACT_COMBINE =
sig
```

end

Task 1.1 (0 pts). Before the support code will load, you need to copy your solutions from HW9 into the appropriate spots in dict.sml, which is an implementation of dictionaries with some extra operations that you might find useful. If you didn't finish HW09, you can contact me for a reference implementation.

Task 1.2 (25 pts). Implement this module in extractcombine.sml.

This should be an abstraction of your frequencies solution from HW9.

You do not need to write tests for extractcombine. You can test by running the word frequency counting code in wordfreq.sml after loading the CM file sources-ec.cm. For example:

```
- CM.make "sources-ec.cm";
- WordFreq.test();
```

Task 1.3 (0 pts). Make sure CM.make "sources-ec-file.cm"; also loads without errors — otherwise you are assuming that the data source MR is a sequence, and your extract-combine code won't also work for files. If it doesn't, rewrite your extractcombine so that the only operation it applies to the 'a MR.mapreduceable is MR.mapreduce.

2 Text Classification

See the section on testing below for which CM files to use to compile your code for this part.

In this problem, you will implement a simple form of *statistical machine learning*—i.e. you will write a computer program that learns from examples. Machine learning techniques are ubiquitous these days; they play a role in web search, touchscreen input recognition, voice recognition, machine translation; sports and election and economic predictions, . . . Our goal for this assignment is to categorize text documents in some way. Specifically, we will organize Reuters news articles into four categories used by Reuters: (CCAT = "corporate/industrial", ECAT = "economics", MCAT = "market", GCAT = "government/social"). Such a categorization might be used by a news aggregator site to automatically group articles by topic. The same idea can be used to implement spam filters (the categories are "spam" and "not spam"), to recognize what language a web page is in, and for many other purposes.

In (supervised) machine learning, the starting point is some training examples, which have been labeled with the correct outputs by some means (e.g. hand-labeled by a person). Based on the training examples, you build some sort of statistical model, which is then used to predict the output for new examples. The model's predictions are tested on some test examples, which are also labeled, but are not included in the training examples.

For this assignment, we will be using a collection of Reuters news articles from the late 1990s that have been labeled with one of the above four categories.³.

²These are the top level of a hierarchical categorization scheme; we will ignore all the lower levels.

³Lewis, Yang, Rose, and Li. RCV1: A New Benchmark Collection for Text Categorization Research. Journal of Machine Learning Research, 2004.

MCAT	Worries about the U.SIraq crisis faded on Asian markets
CCAT	Sun Microsystems Inc president Ed Zander will sign on June 16
GCAT	Israel's beleaguered leader Benjamin Netanyahu scored a
ECAT	International trade through Florida totaled \$26.9 billion
ECAT	Nothing is sacred, it appears, in the British Treasury's
GCAT	The following is a list of upcoming ballot initiatives

The goal is to build a classifier that, given a new article, labels it with one of MCAT or CCAT or ECAT or GCAT.

We have provided training and test datasets, each with 70,000–80,000 labeled articles.

2.1 Naïve Bayesian classification

We write P(A) for the probability of something, and $P(A \mid B)$ for the conditional probability of thing A assuming that B happened. One form of Bayes' rule is that,

$$P(A \mid B)$$
 is proportional to $P(A) \times P(B \mid A)$

Bayes' rule is used to "flip" a conditional probability $P(A \mid B)$, expressing it in terms of $P(B \mid A)$ and some estimate of how likely A is outright.

For categorization, we would like to know

how likely is it that a document has category C, given that the document words are w_1, \ldots, w_n ?

because then we can choose the most likely category. Applying Bayes' rule with A = "document has category C" and B = "document has words w_1, \ldots, w_n ?", the probability we want is proportional to

how likely is a document to have category C? (without knowing anything about what is in the document)

and

how likely is it for a document in category C to be the words w_1, \ldots, w_n ?

This is helpful because we can extract information from the training data that allows us to answer these questions:

• To know how likely a document is to have category C, we count how many documents are in each category, and the total number of training documents:

 $P(a mtext{ document has category } C) = \frac{\text{number of documents with category } C}{\text{total number of categorized documents}}$

• To know how likely a document in category C is to be w_1, \ldots, w_n , we make the naïve assumption that all words are independent, so that

$$P(\text{document in category } C \text{ is } w_1, \dots, w_n) = \prod_{i=1}^n P(\text{word in category } C \text{ is } w_i)$$

For the latter, we count the number of times each word occurs in each category, and the total number of words in each category:

$$P(\text{word in category } C \text{ is } w_i) = \frac{\text{number of times } w_i \text{ occurs in documents with category } C}{\text{number of words in documents with category } C}$$

Putting this all together, we get:

$$P(C \mid w_1, \dots, w_n) = \frac{\text{number of docs in } C}{\text{total number of docs}} \cdot \prod_{i=1}^n \frac{\text{count of } w_i \text{ in } C}{\text{total number of words in } C}$$

One technical point is that the above probabilities often get too small to represent in a floating point number. Because the natural log function is monotone, it is equivalent (because log turns products into sums) to compute:

$$\ln P(C \mid w_1, \dots, w_n) = \ln \frac{\text{number of docs in } C}{\text{total number of docs}} + \sum_{i=1}^n \ln \frac{\text{count of } w_i \text{ in } C}{\text{total number of words in } C}$$

and then take the max of these. This keeps the numbers in a range that is easier to represent.

Another point is what to do about a word that occurs in the test document that does not appear in the training documents (so we have no idea how likely it is). There are several possibilities, but one that works well is to say that its probability is

$$\ln\left(\frac{1}{\text{total number of unique words in all training documents}}\right)$$

Overall, we have the following algorithm:

- 1. Training: from the training examples, compute the quantities used above.
- 2. Classifying: compute $\ln P(C \mid w_1, \dots, w_n)$ for each category C, and then classify with the category C that maximizes this probability.

The assumption behind this algorithm is that we have a representative collection of training examples, so that the distribution of words the training examples will predict the categories for test examples.

2.2 Task

A category is just a string, a document is a sequence of words, and a labeled_document is a document (sequence of words) together with a category. The main export is the train_classifier function, which is given a training dataset of labeled documents, and produces a classifying function.

However, to make it easier to test the intermediate stages of the computation, your classifier will also export the intermediate functions described in the NAIVE_BAYES_CLASSIFIER signature. For everyone but the tester, we will retype the classifier with the CLASSIFIER signature given above to hide the helper functions.

2.2.1 Training

From the training data, you need to extract the following information:

- 1. for each category, the number of documents in that category
- 2. for each category, the total number of words in that category (counting duplicates)
- 3. for each category and word, the number of times that word occurs in documents with that category
- 4. the sequence of all categories
- 5. the total number of classified documents
- 6. the total number of distinct words used in all documents (i.e. don't count duplicates).

You will probably want to use multiple extract-combines to do this (my solution uses four or five).

Task 2.1 (30 pts). Use ExtractCombine.extractcombine to define a function

```
type statistics =
        (category,int) Dict.dict
   * (category,int) Dict.dict
   * (category * string, int) Dict.dict
   * category Seq.seq
   * int
   * int
```

val gather: labeled_document MR.mapreducable -> statistics Feel free to also use any functions from the DICT and SEQUENCE signatures.

2.2.2 Classifying

Now we use the above data to classify a given document.

Task 2.2 (20 pts). First, compute the log-probabilities of each category. Define a function

```
val possible_classifications : statistics * document -> (category * real) Seq.seq
```

that maps a document w_1, \ldots, w_n to the sequence of all pairs

$$(C, \ln P(C \mid w_1, \dots, w_n))$$

for every category C. The Math.ln function computes the natural log.

Task 2.3 (10 pts). Next, compute the best (maximum) category:

```
val classify : statistics * document -> category * real
```

The function can return the empty string and Real.negInf (negative infinity) if there are no possible classifications.

2.2.3 Putting it all together

Task 2.4 (10 pts). Finally, define

For efficiency, it is important that this function does all processing of the training data is done before the document -> category * real function is returned. This is something we can do with a function-that-returns-a-function that we could not do if the function took in a pair labeled_document MR.mapreducable * document as input. Training will sometimes take minutes, and you definitely do not want to retrain the classifier for every document that you classify.

```
signature NAIVE_BAYES_CLASSIFIER =
sig
   type category = string
   type labeled_document = category * string Seq.seq
   type document = string Seq.seq
   val train_classifier : labeled_document MR.mapreducable -> (document -> (category * real))
   (* ------ *)
   (* internal components that are exported only for testing *)
   type statistics =
         (category,int) Dict.dict
       * (category,int) Dict.dict
       * (category * string, int) Dict.dict
       * category Seq.seq
       * int
       * int
   val gather : labeled_document MR.mapreducable -> statistics
   val possible_classifications : statistics * document -> (category * real) Seq.seq
   val classify : statistics * document -> category * real
```

Figure 1: Classifier signature

end

2.3 Testing

Testing Each Function For these tests, you should compile your code with

```
- CM.make "sources-classify-seq.cm";
   We have provided test functions for printing out each stage of the computation:
val print_stats
                          : labeled_document MR.mapreducable -> unit
val print_stats_nofreqs : labeled_document MR.mapreducable -> unit
                          : labeled_document MR.mapreducable * labeled_document -> unit
val print_possibles
val number_correct
                          : labeled_document MR.mapreducable
                          * labeled_document MR.mapreducable
                          -> int * int
val print_predictions
                          : labeled_document MR.mapreducable
                          * labeled_document MR.mapreducable
                          -> unit
   The outputs look like this:
   • Print stats
    - TestSeq.print_stats TestSeq.dups_train;
    Number of documents by category:
       ECAT 1
       GCAT 1
    Number of words by category:
      ECAT 4
       GCAT 4
    Frequencies:
       ECAT: price occured 2 times
      ECAT: stock occured 2 times
       GCAT: congress occured 2 times
       GCAT: court occured 2 times
    All categories: ECAT GCAT
    Total number of documents:2
    Total number of distinct words:4
  • Print possibles:
    - TestSeq.print_possibles (TestSeq.dups_train, TestSeq.doc4);
    Given Categories: ECAT
    Scores:
      ECAT ~2.77258872224
```

GCAT ~3.4657359028

This shows the given category of the document (i.e. the ones it was labeled with), and the scores the classifier returned for each category. The classifier got things right when the maximum score is the given category (note that the numbers are negative, so maximum is closest to 0).

• Print predictions:

```
- TestSeq.print_predictions (TestSeq.dups_train, TestSeq.docs14);
CORRECT
Given Categories: ECAT
Predicted: ECAT
stock
CORRECT
Given Categories: GCAT
Predicted: GCAT
congress
CORRECT
Given Categories: GCAT
Predicted: GCAT
court fell
CORRECT
Given Categories: ECAT
Predicted: ECAT
```

For each document in a sequence, print the given category (what it was labeled with), the predicted category, and the document.

• Number correct:

stock ticker

```
- TestSeq.number_correct (TestSeq.simple_train, TestSeq.docs14);
val it = (4,4) : int * int
```

For each document in a sequence, run the classifier, and compute the pair (number correctly classified, total number of documents).

We have also provided very small documents in the TestSeq module in testclassify.sml.

```
Task 2.5 (0 pts). The files
expected-outputs/stats.txt
expected-outputs/possibles.txt
expected-outputs/predictions.txt
expected-outputs/number-correct.txt
```

show many ways to call to these test functions and what they should output. Make sure your code matches these outputs (up to floating point rounding errors).

Evaluating your classifier For these tests, you should compile your code with

- CM.make "sources-classify-file.cm";

Now, you should run your classifier on some real data. Download hw10data.tar and unzip it to create a data directory inside your hw10-handout folder. We have provided files of three sizes:

```
Num docs File

65 RCV1.small_train.txt
8 RCV1.small_test.txt

7356 RCV1.medium_train.txt
808 RCV1.medium_test.txt

72398 RCV1.big_train.txt
78899 RCV1.big_test.txt
```

You should evaluate your classifier by counting the number it gets correct, such as:

```
TestFile.number_correct (TestFile.open_file "data/RCV1.small_train.txt", TestFile.open_file "data/RCV1.small_test.txt");
```

Each run should take no more than 10–20 minutes.

The small test is small enough that you can print out the results to look at them:

```
TestFile.print_predictions (TestFile.open_file "data/RCV1.small_train.txt", TestFile.open_file "data/RCV1.small_test.txt");
```

Task 2.6 (5 pts). In a comment at the bottom of classify.sml, report the percentage your classifier gets correct for each of the three sizes (small, medium, large). You can also use training/test of mismatched sizes to investigate how much additional training data helps—e.g. does using the big training data improve results on the medium test?