

Comp 212^{ab}

Functional Programming

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Parallelism



Hardware

① Multicore CPUs/
processor (+)

OLD: CPUs do one thing at a time

NEW: many laptop 2 cores
4 cores
8 cores
16 cores

② GPUs (graphics)

↳ 1000s of things at once

③ Data centers

10,000s of computers

16-32-64 cores

Parallel Functional Programming

- Say what is to be computed
at a high level
- let the compiler assign
work to processors

(* Purpose: count the number of people who took 211 in Python *)

type class = row sequence
fun count(c : class) : int =

sum (② map sum c) ↖ int sequence
①

① in parallel, sum each row

② sum the column at the end

(* Purpose: add up a row *)

type row = int sequence

sum : row \rightarrow int

(* Example:

sum <1,1,0,1,1> = 5 *)

Computing by calculation

val row1: row = <1, 1, 0, 1, 1>

val row2: row = <0, 1, 1, 0, 1>

val class = <row1, row2>

Count class

runs by stepping through
the definitions of the
functions

count (row1, row2)

↳ sum (map sum (row1, row2))

↳ sum (< sum row1, sum row2 >)

↳ sum (< 4 , 3 >)

↳ 4 + 3

↳ 7

mathematical
definition
of what it
means to run
a program

You will learn to:

- ① write parallel functional programs
- ② analyze their sequential and parallel running times

Suppose classroom n students
in n rows

$n \times n$

Sequential : $\approx n^2$ $O(n^2)$
(work) \rightarrow 1 processor

Parallel : $\approx n$ n $\approx n$
step 1 + step 2
(span) \rightarrow "enough" processors
infinite

work and span predict

The running time with
 P processors

for any P

via

Brent's Principle

time on p processors

$$\approx \approx \max\left(\frac{\text{Work}}{p}, \text{Span}\right)$$

$n = 10$ 100 students

$$\text{Work} = 100$$

$$\text{Span} = 10$$

$$p = 2 \quad \frac{\text{Work}}{p} = 50$$

$$\max\left(\frac{W}{p}, S\right) = \overset{\text{max}}{(50, 10)} \\ = 50$$

$$P = 100$$

$$\frac{W}{P} = 1$$

$$S = 10$$

$$M^x(1, \underline{10}) = 10$$

You will learn to:

- ① write parallel functional programs
- ② analyze their sequential and parallel running times
- ③ reason mathematically about their correctness
- ④ structure large programs using abstract types

sum: int sequence \rightarrow int



sum faster: int sequence \rightarrow int

Theorem: for all s: int sequence,

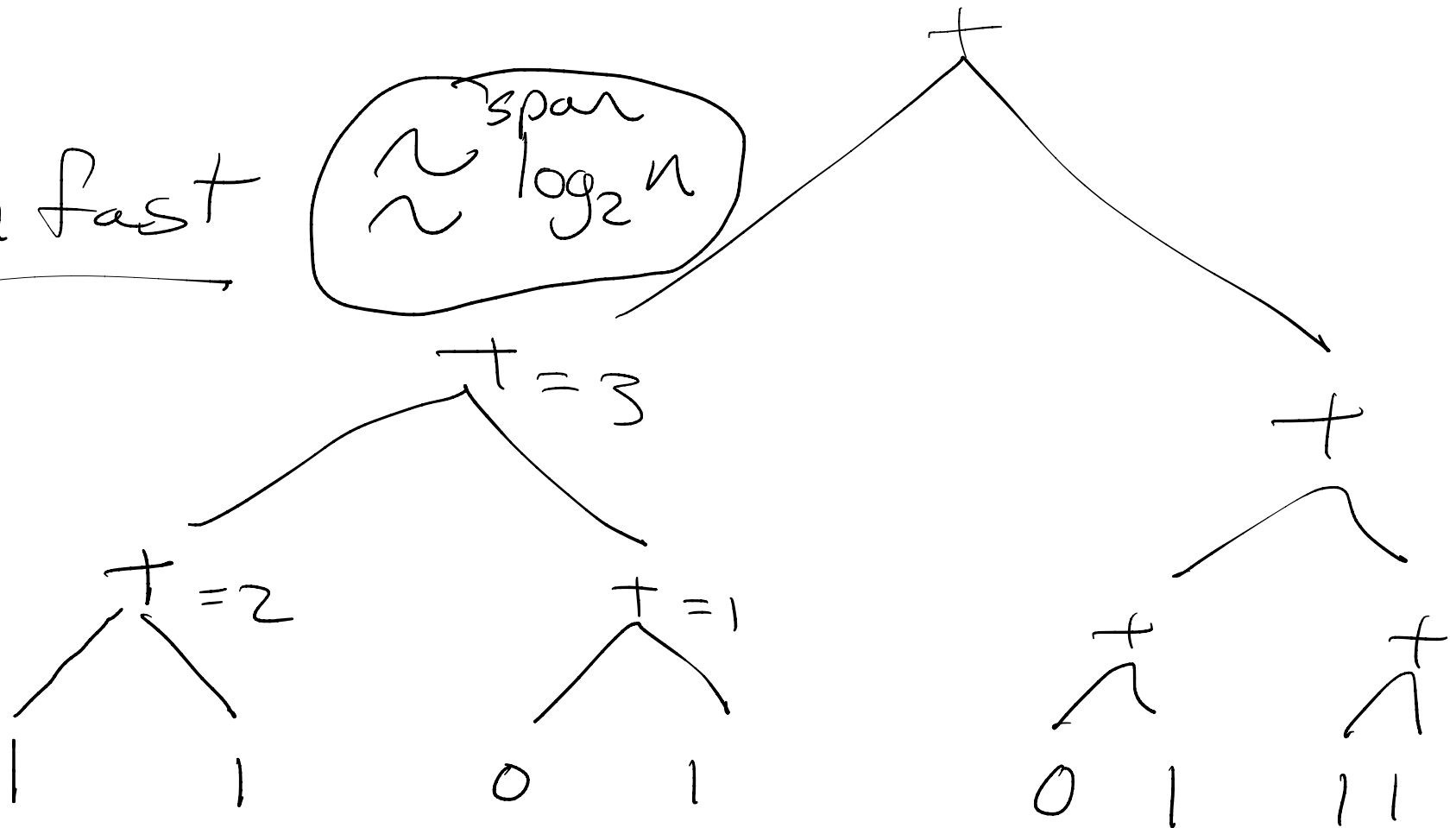
$$\underline{\underline{\text{sum}(s) == \text{sumfast}(s)}}$$

Sum has span $\approx n$ (length of row)

$$1 + (1 + (0 + 1))$$

Sum Fast

span
 $\approx \log_2 n$



Activities

① pre-recorded/asynch lectures

② labs weekly

Th	1pm
Th	2:50pm
Fri	1pm

③ Homework

Wed	1pm
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+ help sessions

↳ due Thursday before labs
(?)

Assessment

5% labs

95% homework

↳ regular → help

↳ challenge → no help